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bessel functions first defined by the mathematician daniel bernoulli and then generalized by friedrich bessel are canonical solutions y x of bessel s differential equation for an arbitrary complex number which represents the order of the bessel function the bessel functions of the first kind j n x are defined as the solutions to the bessel differential equation x 2 d 2y dx 2 x dy dx x 2 n 2 y 0 1 which are nonsingular at the origin they are sometimes also called cylinder functions or cylindrical harmonics bessel function are an inexhaustible subject there are always more useful properties than one knows in mathematical physics one often uses specialist books 3 bessel function the bessel function j s z is de ned by the series j s z z 2 sx1 k 0 1 k k s k 1 z 2 2k 29 this series converges for all zon the complex plane thus j s z is the entire function if z 0 then j s z z 2 s 1 s 1 30 if s2 is not an integer then j s z is the second solution of the bessel equation now j s bessel function any of a set of mathematical functions systematically derived around 1817 by the german astronomer friedrich wilhelm bessel they arise in the solution of laplace s equation when the latter is formulated in cylindrical coordinates the bessel functions of semi integer order we now con sider the special cases when the order is a a semi integer number n 1 2 n 0 1 2 3 in these cases the standard bessel function can be expressed in terms of elementary functions a bessel function is a function defined by the recurrence relations 1 and 2 the bessel functions are more frequently defined as solutions to the differential equation 3 there are two main classes of solution called the bessel function of the first kind and bessel function of the second kind bessel s equation arises when finding separable solutions to laplace s equation and the helmholtz equation in cylindrical or spherical coordinates this function is called the bessel function of the rst kind of order one can easily show that the radius of convergence of the power series at the end of 12 is in nite so the power series converges for all complex x bessel functions arise in many problems in physics possessing cylindrical symmetry such as the vibrations of circular drumheads and the radial modes in optical fibers they also provide us with another orthogonal set of basis functions introduction to the bessel functions general the bessel functions have been known since the 18th century when mathematicians and scientists started to describe physical processes through differential equations many different looking processes satisfy the same partial differential equations a second linearly independent solution can be found via reduction of order when appropriately normalized it is denoted by yp x and is called the bessel function of the second kind of order p the general solution to bessel s equation is y c1jp x c2yp x the bessel functions have been known since the 18th century when mathematicians and scientists started to describe physical processes through differential equations many different looking processes satisfy the same partial differential equations the best known properties and formulas for bessel functions real values for real arguments for real values of parameter and positive argument the values of all four bessel functions and are real simple values at zero the bessel functions and have rather simple values for the argument chapter 10 bessel functions f w j olver institute for physical science and technology and department of mathematics university of maryland college park maryland l c maximon center for nuclear studies department of physics the george washington university washington d c this chapter is based in part on abramowitz and stegun 1964 bessel equations and bessel functions bessel functions form a class of the so called special functions they are im portant in math as well as in physical sciences physics and engineering they are especially important in solving boundary values problems in cylindrical coordi nates first we define another important function the gamma the modified bessel function of the first kind is implemented in the wolfram language as besseli nu z the modified bessel function of the first kind i n z can be defined by the contour integral i n z 1 2pii e z 2 t 1 t t n 1 dt 1 where the contour encloses the bessel function of order u in mathbb c can be defined when u is not a negative integer via the series begin equation label e series j u z sum k 0 infty frac 1 k gamma k 1 gamma k u 1 left frac z 2 right u 2k left frac z 2 right u sum k 0 infty frac 1 k gamma k 1 gamma one solution of the differential equation is the bessel function of the first kind of order p given as y x j p x sum n 0 infty dfrac 1 n gamma n 1 gamma n p 1 left dfrac x 2 right 2 n p label 7 39 symbols j ν z bessel function of the first kind y ν z bessel function of the second kind π the ratio of the circumference of a circle to its diameter f x partial derivative of f with respect to x x partial differential of x n integer z complex variable and ν complex parameter

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the bessel function of order u in mathbb c can be defined when u is not a negative integer via the series begin equation label e series j u z sum k 0 infty frac 1 k gamma k 1 gamma k u 1 left frac z 2 right u 2k left frac z 2 right u sum k 0 infty frac 1 k gamma k 1 gamma

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one solution of the differential equation is the bessel function of the first kind of order p given as y x j p x sum n 0 infty dfrac 1 n gamma n 1 gamma n p 1 left dfrac x 2 right 2 n p label 7 39

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